

GUJARAT TECHNOLOGICAL UNIVERSITY

BACHELOR OF ENGINEERING – SEMESTER 7 – EXAMINATION – SUMMER 2026

Subject Code: 3172008

Date: 29/05/2026

Subject Name: Finite Element Analysis

Time: 02:30 PM TO 05:00 PM

Total Marks: 70

Instructions:

- 1. Attempt all questions.**
- 2. Make suitable assumptions wherever necessary.**
- 3. Figures to the right indicate full marks.**
- 4. Simple and non-programmable scientific calculators are allowed.**

- Q.1**
- (a) Define the Finite Element Method and list its main advantages over other numerical methods. **03**
 - (b) Explain how boundary conditions are applied in FEM. **04**
 - (c) Derive the stiffness matrix for a 2-spring system connected in series using the potential energy method. **07**

- Q.2**
- (a) A linear spring has stiffness 800 N/m and is subjected to a 50 N force. Find the displacement at the free end. **03**
 - (b) Derive the stiffness matrix for a 1D bar using the potential energy approach. **04**
 - (c) For a 2-element spring system with stiffnesses $k_1 = 100$ N/mm and $k_2 = 200$ N/mm connected in parallel under 30 N load, determine total stiffness and displacement. **07**

OR

- Q.2**
- (c) Explain the concept of isoparametric elements, and derive 1D isoparametric formulation. **07**
- Q.3**
- (a) Write down the global stiffness matrix for a bar element in plane coordinates. **03**
 - (b) A bar of length 300 mm is made of aluminum ($E = 70$ GPa, $A = 100$ mm²) and carries a 5 kN load at the free end. Find elongation and stress. **04**
 - (c) Derive and explain transformation and stiffness matrices for a 3D truss member. **07**

OR

- Q.3**
- (a) Explain the use of symmetry in structural analysis. **03**
 - (b) Differentiate between lumped mass and consistent mass matrices. **04**
 - (c) A single degree of freedom system has $k = 4000$ N/m, $m = 50$ kg, and damping $c = 100$ Ns/m. Find natural frequency, damping ratio, and damped frequency. **07**

- Q.4**
- (a) Define natural frequency and mode shape. **03**
 - (b) A system has stiffness $k = 2000$ N/m and mass $m = 10$ kg. Determine natural frequency in rad/s and Hz. **04**
 - (c) Derive the equations of motion for a finite element dynamic system. **07**

OR

- Q.4**
- (a) Two springs with stiffness $k_1 = 50$ N/mm and $k_2 = 100$ N/mm are connected in series. Derive the global stiffness matrix for this assembly. **03**
 - (b) Explain the concept of 'Shape Functions' and state the characteristics they must satisfy for a 1D bar element. **04**

- (c) A stepped bar is subjected to an axial load of 100 kN. Section 1: $L = 300 \text{ mm}$, $A = 500 \text{ mm}^2$ Section 2: $L = 200 \text{ mm}$, $A = 300 \text{ mm}^2$ $E = 200 \text{ GPa}$ for both. One end is fixed. Calculate the nodal displacements, stresses in each section, and reaction forces. **07**

- Q.5** (a) State the properties of a Global Stiffness Matrix. **03**
(b) Compare Constant Strain Triangle (CST) and Linear Strain Triangle (LST) elements in terms of convergence and accuracy. **04**
(c) Explain Isoparametric, Sub-parametric, and Super-parametric elements with neat sketches. **07**
Why is the Isoparametric formulation preferred in commercial FEM software like ANSYS?

OR

- Q.5** (a) Explain why the global stiffness matrix is always a symmetric and banded matrix. **03**
(b) Describe the Penalty Method used for applying boundary conditions in FEM. **04**
(c) A 2D truss element is oriented at 45° to the global x-axis. If the local stiffness is $k = AE/L$, find the global stiffness matrix for this single element. **07**
