

GUJARAT TECHNOLOGICAL UNIVERSITY**BE - SEMESTER-IV(NEW) EXAMINATION – WINTER 2022****Subject Code:3140912****Date:14-12-2022****Subject Name:Electromagnetic Fields****Time:10:30 AM TO 01:00 PM****Total Marks:70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Simple and non-programmable scientific calculators are allowed.

MARKS

- Q.1** (a) Explain how cross product of vectors can be obtained. Does cross product obey the commutative law? Comment **03**
- (b) A certain vector F is given by $F = -5a_x - a_y(3x+2) + a_z$. Find |F| and unit vector in the direction of F **04**
- (c) Discuss cylindrical and spherical co-ordinate system of vectors. Also explain how a vector in Cartesian co-ordinate system can be converted into cylindrical and spherical system. **07**
- Q.2** (a) State Coulomb's law and hence define electric field intensity **03**
- (b) If $Q_1 = 3 \times 10^{-4} \text{ C}$ is located at M (1,2,3) and $Q_2 = -10^{-4} \text{ C}$ is located at N(2,0,5) in vacuum, find the vector force on Q_2 by Q_1 using Coulomb's law **04**
- (c) Derive the equation for electric field intensity due to uniform sheet charge located at $z = 0$ plane at any point on the positive z-axis. What do you infer from the result obtained? **07**
- OR**
- (c) Determine the total charge (i) on cylinder $\rho = 3$, $0 < z < 4$, if $\rho_s = \rho z^2 \text{ nC/m}^2$. (ii) within the sphere if $\rho_v = 10/r \sin\theta \text{ C/m}^3$ **07**
- Q.3** (a) State and explain Gauss' law. **03**
- (b) An infinite line charge on the z-axis passes through the centre of the cylinder (having radius ρ) which is lying on the $z = 0$ plane. Using Gauss' law, find the total charge enclosed **04**
- (c) Discuss the application of Gauss' law to differential volume element and hence explain divergence theorem **07**
- OR**
- Q.3** (a) State the expression for work done in carrying a point charge from one place to another in an electric field. Hence, define potential difference. **03**
- (b) In the region of free space that includes the volume, $2 < x, y, z < 3$ and $D = \frac{2}{z^2} (yza_x + xza_y - 2xya_z) \text{ C/m}^2$, find the total charge enclosed using divergence theorem. **04**
- (c) Define potential gradient. Prove that $E = -\text{grad } V$ **07**
- Q.4** (a) State the point form of Ohm's law **03**
- (b) Derive the continuity equation $\nabla \cdot J = -\frac{\partial \rho_v}{\partial t}$ **04**
- (c) State and explain uniqueness theorem **07**
- OR**
- Q.4** (a) State and explain Biot Savart's law **03**

- (b) Starting from the point form of Gauss' law, derive Poisson's and Laplace's equations **04**
- (c) Given the vector magnetic potential $A = -\rho^2/4 a_z \text{ Wb/m}^2$, calculate the total magnetic flux crossing the surface, $\Phi = \pi/2$, $1 < \rho < 2\text{m}$, $0 < z < 5\text{m}$. **07**
- Q.5** (a) State and explain Lorentz force equation **03**
- (b) Explain the term 'displacement current' in brief **04**
- (c) For uniform magnetic field intensity, prove that torque on a closed circuit is given by the cross product of magnetic dipole moment and flux density. **07**
- OR**
- Q.5** (a) Explain Stoke's theorem in brief. **03**
- (b) Explain in brief, different types of magnetic materials **04**
- (c) Discuss Maxwell's equations in integral form and point form. Explain how they relate and electric and magnetic fields with each other. State applications of the same **07**
